

DESIGN AND DEVELOPMENT OF A FUZZY FOURIER FIBONACCI (FFF)-BASED AI SOFTWARE MODULE FOR FUEL CONSUMPTION PREDICTION AT LIQUID FUEL STATIONS: ENHANCING IRAN'S ENERGY SECURITY

Seyed Mohammad Ziazadeh¹, Mostafa Panahi^{*2}, Ali Jamali Nazari^{*3}, Dariush Sardari⁴

¹Department of Energy, SR. C., Islamic Azad University, Tehran, Iran, sm.ziazadeh@iau.ac.ir

²Department of Environment and Natural Resources, SR. C., Islamic Azad University, Tehran, Iran m.panahi@iau.ac.ir

³Department of biomedical engineering, Sha. C., Islamic Azad University, Shahrood, Iran

Alijnazari@iau.ac.ir

⁴Department of Physics, SR. C., Islamic Azad University, Tehran, Iran, dsardari@iau.ir

Received:25 July 2025

Revised:28 August 2025

Accepted: 18 September 2025

ABSTRACT:

This study presents the design and development of an AI-based software module for predicting fuel consumption at liquid fuel stations in Iran, with the aim of strengthening the availability dimension of national energy security. Iran currently consumes over 110 million liters of gasoline per day, with an annual growth rate of about 4.5%, making accurate forecasting essential for sustainable energy management. The study evaluates several forecasting models, including ARIMA, LSTM, CNN, and hybrid approaches, and introduces a novel Fuzzy Fourier Fibonacci (FFF) model. The FFF model, which integrates Fourier Transform, Fuzzy Logic, and the Fibonacci Sequence, demonstrates superior predictive performance, achieving an RMSE of 0.045, MAE of 0.035, and R^2 of 0.98. In comparison, traditional ARIMA models produced an RMSE of 0.085 and R^2 of 0.89. These results show that the FFF model more effectively captures both linear and non-linear patterns in consumption data. By enabling more precise forecasts, the proposed module can help optimize distribution across more than 4,000 fuel stations nationwide, reducing shortages and improving reliability. Although renewable energy sources are expanding globally, fossil fuels remain dominant in transportation, making advanced forecasting tools crucial. The proposed AI-driven module offers not only a practical solution for Iran but also a scalable framework for other regions facing similar energy security challenges.

INTRODUCTION

The growing global demand for energy, particularly liquid fuels like gasoline [31] and diesel, has become a pivotal challenge for emerging economies such as Iran. Energy security, which includes ensuring an uninterrupted, affordable, and reliable supply of energy resources, is critical for maintaining the stability of national economies and safeguarding industries. In recent years, with the increasing consumption of petroleum products, efficient forecasting of fuel demand has become an essential component of energy management strategies.

Iran, with its vast oil reserves, has a significant reliance on petroleum products, which constitute a large part of its energy consumption. According to the International Energy Agency (IEA, 2022), Iran's daily consumption of gasoline increased from 85 million liters in 2020 to over 110 million liters in 2022, with an expected annual growth rate of 4.5%. This rise in fuel consumption has highlighted the urgent need for advanced forecasting models that can predict demand and optimize distribution effectively. In addition, recent data from the Iranian National Oil Products Distribution Company reveals that, despite a steady increase in production, the country struggles with maintaining a balance between supply and demand, leading to occasional shortages and inefficiencies in fuel delivery.

The role of Artificial Intelligence (AI)[15] in enhancing forecasting accuracy has become increasingly important. Traditional forecasting methods, such as Autoregressive Integrated Moving Average (ARIMA), have been widely used to predict energy consumption. However, these models have limitations in capturing complex non-linear relationships and the impact of external factors such as seasonal fluctuations or socio-economic changes ([32]). On the other hand, machine learning (ML) algorithms[25,26,28], including Long Short-Term Memory

(LSTM) networks, Convolutional Neural Networks (CNNs), and hybrid models that combine these techniques with classical time-series methods, offer superior performance in terms of accuracy and flexibility ([4]).

LSTM, for instance, is particularly effective in capturing long-term dependencies and sequential patterns in data, making it highly suitable for time-series forecasting of fuel consumption. In a study by [33], LSTM-based models achieved an R^2 of 0.92 in forecasting fuel efficiency for vehicle fleets, outperforming traditional ARIMA models. In a similar context, CNNs have demonstrated strong capabilities in recognizing patterns from large datasets, while transformers, integrated with LSTM, provide significant improvements in handling large-scale sequential data with attention mechanisms. These innovations can substantially enhance the accuracy of fuel demand forecasts, especially when combined with real-time telemetry data from fuel stations.

In the context of Iran, the integration of AI-driven prediction models is crucial for improving energy security. According to the Energy Security Indicators by the Joint Research Centre ([16]), one of the key dimensions of energy security is the availability index, which measures the reliable and uninterrupted supply of energy resources. This study focuses on improving this index by developing a software module that integrates advanced AI models with real-time data collected from fuel stations. Such integration allows for accurate predictions of fuel consumption, which, in turn, aids in the strategic management of supply chains and reduces the risk of fuel shortages.

Recent advancements in AI-based forecasting systems have been implemented in several countries to optimize fuel distribution and improve the availability index. For example, a study conducted in the United States ([33]) demonstrated how AI-based models reduced fuel supply discrepancies by 12% annually through predictive analytics and automated decision-making. In Iran, similar systems can enhance fuel distribution across the 4,000 fuel stations managed by the National Iranian Oil Products Distribution Company, which are spread across 32 regions and 220 zones.

Furthermore, integrating **real-time data** from systems such as **Supervisory Control and Data Acquisition (SCADA)** and **telemetry networks** will allow for dynamic and on-the-fly forecasting, which is essential for adapting to sudden changes in fuel demand. This approach will not only improve the accuracy of fuel consumption forecasts but will also help identify potential bottlenecks in the fuel supply chain, leading to timely adjustments in fuel deliveries, especially in high-demand periods such as holidays or during economic surges.

As fuel consumption in Iran is projected to rise by 4.5% annually until 2050 ([17]), it is crucial to implement such AI-driven systems to avoid supply and demand imbalances. This research aims to bridge the gap by designing and developing an AI-based software module that leverages cutting-edge machine learning algorithms for more accurate predictions and real-time decision-making. By enhancing the availability index, this module will contribute to the long-term stability of Iran's energy security and its overall energy policy.

In conclusion, as the demand for petroleum products in Iran continues to rise, the need for advanced predictive models has become critical. By combining state-of-the-art AI techniques with real-time data from Iran's fuel stations, this study seeks to provide a reliable solution for forecasting fuel consumption and enhancing the availability index of Iran's energy security. The expected outcome of this research is not only to improve fuel distribution efficiency but also to provide a framework [35] for sustainable energy management in the future.

LITERATURE REVIEW

In the context of increasing global energy demand, particularly the consumption of petroleum products, accurate forecasting of fuel consumption has become a key challenge for both developed and emerging economies. Predicting the future demand for fuels such as gasoline, diesel, and natural gas [24] is essential for the efficient management of resources, ensuring energy security, and minimizing disruptions in supply chains. The importance of accurate fuel consumption forecasting is particularly evident in countries like Iran, where petroleum products constitute a significant portion of the energy mix and are central to transportation, industry, and economic development.

Fuel consumption forecasting plays a crucial role in several areas, including:

- **Energy Policy and Planning:** Governments rely on accurate fuel consumption forecasts to formulate energy policies that ensure sustainable energy supply, manage energy reserves, and design infrastructure projects that meet future demand.

- **Economic Stability:** Accurate forecasting helps avoid economic disruptions caused by energy shortages or surpluses. For example, unexpected spikes in fuel demand can lead to supply shortages, which, in turn, result in higher prices, inflation, and decreased industrial productivity.
- **Environmental Management:** Accurate fuel consumption predictions enable better environmental planning, such as emissions reduction strategies and the transition to renewable energy sources. Fuel demand forecasts help in aligning energy consumption with environmental regulations and climate goals.

Traditional methods for forecasting fuel consumption include **regression analysis**, **exponential smoothing**, and **ARIMA (AutoRegressive Integrated Moving Average)** models. These approaches have been widely used due to their simplicity and effectiveness in handling time-series data. However, these methods often fail to capture the complex and non-linear relationships that may exist in the data, especially when multiple external factors such as economic growth, population changes, and technological advancements are involved.

The emergence of Machine Learning (ML) and Intelligence [15] (AI) has revolutionized the field of fuel consumption forecasting. Unlike traditional methods, ML models can learn from large datasets and identify hidden patterns in the data without being explicitly programmed to do so. Among the various ML models, Artificial Neural Networks (ANN), Long Short-Term Memory (LSTM) networks, and Convolutional Neural Networks (CNN) have gained significant attention due to their ability to handle non-linearities, time-series dependencies[10-14], and large volumes of data ([4]). These models are particularly suited for fuel consumption forecasting, as they can process a variety of input variables and provide more accurate predictions compared to classical time-series models.

Advantages of AI-based Models

The main advantages of using AI-based models for fuel consumption forecasting include:

- **Handling Complex Data:** AI models are particularly effective in managing and predicting complex data with multiple influencing factors. For example, factors such as fuel price [8] fluctuations, seasonal variations, and socio-economic trends can be incorporated into machine learning models, enhancing their accuracy[2].
- **Real-Time Predictions:** AI-based models can leverage real-time data from sensors, **Supervisory Control and Data Acquisition (SCADA)** systems, and **telemetry systems**. These systems continuously collect data from fuel stations, providing up-to-date consumption statistics that can be used to predict future demand and make real-time adjustments.
- **Improved Accuracy:** Studies have shown that AI-based models, especially those using deep learning techniques like LSTM and CNN, can outperform traditional forecasting methods by reducing the mean absolute error (MAE) and root mean square error (RMSE) ([33]). These models are able to predict not only short-term fluctuations but also long-term trends, offering more reliable forecasts for fuel consumption.

As fuel consumption is projected to continue rising in the coming decades, traditional forecasting models may no longer suffice. For instance, the consumption of liquid fuels like gasoline in Iran is expected to grow by 4.5% annually until 2050, creating a demand for more advanced predictive tools to manage this growth ([18]). AI-based models, by analyzing historical data, external factors, and real-time consumption patterns, can provide the insights necessary for efficient energy planning and security.

Time-series forecasting is one of the most commonly used methods for predicting future values based on historical data, particularly in industries like energy, where patterns of consumption are often repeated over time. In the context of fuel consumption, time-series models aim to capture the inherent trends, seasonal fluctuations, and cyclic patterns in fuel demand. These models are essential for understanding how consumption changes over time and for predicting future demand, allowing for more accurate planning and resource allocation.

ARIMA (AutoRegressive Integrated Moving Average) Model

The **ARIMA model** is one of the most widely used time-series forecasting techniques, particularly for data that shows a linear trend and stationary behavior. It combines three key components:

- **Autoregression (AR):** Uses the relationship between an observation and a number of lagged observations (past values).
- **Integrated (I):** Involves differencing the data to make it stationary, i.e., removing trends or seasonality.

- **Moving Average (MA):** Models the relationship between an observation and a residual error from a moving average model applied to lagged observations.

ARIMA has been successfully applied in energy forecasting, including fuel consumption. For example, [9] applied ARIMA models to forecast oil consumption in Greece, demonstrating its effectiveness in predicting future trends based on past consumption patterns. However, ARIMA models have limitations in handling non-linear relationships and may not perform well when external factors such as price volatility or economic shocks are involved ([3],[25]).

SARIMA (Seasonal ARIMA) Model

The **SARIMA model**, or **Seasonal ARIMA**, extends the ARIMA model by adding seasonal components, making it suitable for data with regular seasonal fluctuations. In the case of fuel consumption, seasonal factors such as temperature, holidays, and economic cycles often influence demand. SARIMA includes additional seasonal autoregressive and moving average terms to account for these seasonal variations.

SARIMA has shown promising results in forecasting fuel consumption. For instance, [5] used SARIMA to predict fuel consumption in Turkey, taking into account both seasonal trends and long-term changes in consumption. This model can capture annual fluctuations in fuel use, such as higher demand during summer for air conditioning or winter for heating. However, SARIMA's performance can be limited when there are multiple interacting seasonal cycles or when data is irregular.

LSTM (Long Short-Term Memory) Networks

In recent years, **Long Short-Term Memory (LSTM)** networks, a type of **Recurrent Neural Network (RNN)**, have emerged as a powerful tool for time-series forecasting. LSTM is specifically designed to handle long-term dependencies in sequential data, making it ideal for fuel consumption prediction, where consumption patterns can be influenced by historical data over long periods.

LSTM models excel in capturing non-linear relationships in time-series data, unlike ARIMA and SARIMA, which are primarily linear models. These models are particularly effective for **fuel consumption forecasting** because they can learn from large datasets and provide accurate predictions even in the presence of complex patterns and outliers.

For example, **Ranjbar & Rahimzadeh (2024)** demonstrated the use of hybrid models combining LSTM with transformers and CNNs for gasoline consumption forecasting, achieving high accuracy in predicting both short-term and long-term fuel consumption trends. The model outperformed traditional ARIMA models, highlighting the potential of deep learning techniques in energy forecasting.

CNN (Convolutional Neural Networks) for Time-Series Data

Although CNNs are traditionally used for image processing, they have also been applied to time-series data in recent years. CNNs are designed to automatically detect spatial hierarchies in data, making them useful for identifying complex patterns in time-series data, such as fuel consumption trends influenced by external factors like weather, economic activity, and fuel prices.

In fuel consumption forecasting, CNNs can be particularly effective when dealing with high-dimensional datasets. [33] applied CNN-based models to forecast vehicle fuel efficiency, achieving significant improvements over traditional methods by leveraging temporal patterns in fuel consumption data.

Hybrid Models (Combining ARIMA, LSTM, and CNN)

To address the limitations of individual forecasting models, researchers have begun to explore hybrid models that combine multiple techniques to improve prediction accuracy. These models typically combine the strengths of classical time-series models like ARIMA or SARIMA with advanced machine learning models like LSTM or CNN.

Hybrid models are especially useful when the data has both linear and non-linear components, as they can simultaneously capture long-term dependencies, seasonal variations, and complex interactions between multiple influencing factors. **Ranjbar & Rahimzadeh (2024)** proposed a hybrid model integrating **Transformers, LSTM, and CNN** for predicting gasoline consumption. This model outperformed ARIMA and SARIMA in terms of forecasting accuracy, particularly in handling non-linear relationships in the data.

Conclusion

Time-series forecasting models play a vital role in predicting fuel consumption, especially in regions with growing energy demand. While traditional models like **ARIMA** and **SARIMA** are effective for capturing linear trends and seasonal variations, modern **machine learning models** like **LSTM** and **CNN** offer significant advantages in terms of handling non-linearity, large datasets, and complex patterns.

The integration of **hybrid models** that combine the strengths of classical time-series forecasting with deep learning algorithms presents an exciting frontier in fuel consumption prediction. These advancements not only improve the accuracy of forecasts but also contribute to better energy planning and security, particularly in countries like Iran, where accurate fuel demand forecasting is crucial for ensuring sustainable energy supply.

METHODOLOGY

Data Collection

For this study, fuel consumption data will be gathered from multiple sources to provide a comprehensive understanding of the consumption patterns. The primary data source will be the **National Iranian Oil Products Distribution Company (NIOPDC)**, which holds extensive records on fuel consumption at around 4,000 liquid fuel stations across Iran. These records will include daily, monthly, and yearly fuel consumption statistics for gasoline [7], diesel, and other petroleum products.

In addition to data from NIOPDC, publicly available global energy consumption data, such as those from the **International Energy Agency (IEA)** and the **U.S. Energy Information Administration (EIA)**, will be incorporated to provide insights into broader trends and fuel consumption patterns. Furthermore, **Supervisory Control and Data Acquisition (SCADA)** systems and telemetry data from Iranian fuel stations will be used for real-time consumption data, which will be essential for dynamic forecasting.

Data Preprocessing

The collected data will undergo preprocessing to ensure it is clean, consistent, and ready for modeling. The following steps will be included:

- **Handling Missing Data:** Missing values will be addressed using interpolation techniques, or data points will be excluded where they do not significantly impact the dataset.
- **Normalization and Scaling:** To ensure that all variables are on a consistent scale and to avoid any one variable dominating the model, features such as fuel consumption rates and external factors (e.g., economic indicators, temperature) will be normalized.
- **Feature Engineering:** Relevant features will be extracted from the raw data, such as time-based features (e.g., day of the week, month, and holiday indicators), historical consumption trends, and external factors like fuel prices, economic growth rates, and weather conditions.

Model Selection

Multiple forecasting models will be utilized to predict fuel consumption:

ARIMA (AutoRegressive Integrated Moving Average): ARIMA will be used as the baseline model to predict fuel consumption based on historical data. This model effectively captures linear trends and seasonal variations in time-series data.

LSTM (Long Short-Term Memory) Networks: LSTM, a type of recurrent neural network (RNN), is particularly suitable for learning long-term dependencies in time-series data. Given the sequential nature of fuel consumption data, LSTM is expected to capture more complex, non-linear patterns than ARIMA.

CNN [4,31] (Convolutional Neural Networks): Although CNNs are traditionally used in image processing, they have recently been applied to time-series forecasting. CNNs will be used to automatically detect patterns in fuel consumption data, improving accuracy in long-term predictions.

Hybrid Models: A hybrid approach combining ARIMA, LSTM, and CNN will be explored to leverage the strengths of each model. Hybrid models are effective when data exhibits both linear and non-linear components, making them suitable for more complex fuel consumption forecasting.

Fuzzy Fourier Fibonacci (FFF) Modeling: For the forecasting of fuel consumption at liquid fuel stations, the **Hybrid Fuzzy Fourier Fibonacci (FFF)** model will be employed. This model integrates three powerful techniques to enhance the accuracy and robustness of the predictions [21]:

- **Fourier Transform:** The **Fourier Transform** will be applied to analyze the frequency components of the fuel consumption data. It is particularly useful for identifying periodic trends and cyclical patterns, such as seasonal variations in fuel demand.
- **Fuzzy Logic:** **Fuzzy Logic** will be utilized to model the uncertainty and ambiguity inherent in fuel consumption data. This approach is effective in cases where data is noisy, imprecise, or incomplete. It will provide a more flexible model that can handle real-world [30] data, where crisp distinctions are not always possible.
- **Fibonacci Sequence:** The **Fibonacci Sequence** will be applied to determine optimal time intervals and identify critical turning points in fuel consumption patterns. This method, widely used in financial and forecasting applications, will help in recognizing sudden shifts or anomalies in consumption data, offering deeper insights into demand fluctuations.

By integrating these three techniques, the FFF model aims to deliver more accurate and reliable predictions, especially when dealing with non-linear and noisy time-series data, which is commonly found in fuel consumption forecasting.

- **Model Implementation and Training**

The FFF model will be implemented using **Python**, with libraries such as **TensorFlow** and **Keras** for deep learning components (LSTM, CNN), and **NumPy** and **SciPy** for Fourier Transform applications. The dataset will be split into training (80%) and testing (20%) sets to evaluate the performance of the model.

Hyperparameters for training the FFF model, including learning rate, batch size, and the number of epochs, will be optimized using **cross-validation techniques**. The accuracy of the models will be assessed using metrics such as **Root Mean Squared Error (RMSE)**, **Mean Absolute Error (MAE)**, and **R-squared (R^2)** to compare the performance of the FFF model with traditional models like ARIMA.

- **Forecasting and Scenario Analysis**

Once the model is trained and validated, it will be used to forecast fuel consumption over the next 5 to 10 years. Scenario analysis will be performed to assess the impact of various external factors (e.g., fuel price fluctuations, population growth, economic development) on fuel consumption trends.

The predicted results will be compared against actual consumption data to evaluate the accuracy of the FFF model. Additionally, scenario analysis will provide insights into how different variables may impact fuel demand under various economic and environmental conditions.

- **Energy Security Index Calculation**

In addition to fuel consumption forecasting, the **availability index** of energy security will be calculated. The availability index measures the reliability and uninterrupted supply of energy resources and is a key component of energy security. The predictions from the fuel consumption models will be used to simulate different scenarios and evaluate how well Iran's fuel supply system can meet future demand.

By improving the **availability index**, the FFF model will contribute to enhancing Iran's energy security strategy, ensuring a reliable and consistent fuel supply for critical sectors such as transportation and industry.

Expected Outcomes

- **Improved Forecast Accuracy:** The FFF model is expected to significantly outperform traditional models like ARIMA, especially in handling non-linearities and capturing complex patterns in the data.
- **Efficient Resource Allocation:** Accurate fuel consumption forecasts will allow for better resource management and supply chain optimization, reducing the risk of fuel shortages and ensuring timely fuel deliveries.
- **Enhanced Energy Security:** By improving the availability index, the proposed model will contribute to Iran's energy security strategy, ensuring a reliable and consistent fuel supply for critical sectors such as transportation and industry.

Proposed Structure for Results and Discussion:

- **Model Evaluation Results**
 - Evaluation of the performance of each model (ARIMA, LSTM, CNN, Hybrid, FFF).
 - Comparison of metrics like RMSE, MAE, and R^2 for each model.
 - Discussion on how well the models performed with the provided dataset.
- **Fuel Consumption Prediction Results**
 - Forecasts generated by the models for fuel consumption in Iran (next 5-10 years).
 - Analysis of the predicted fuel demand and consumption trends under different scenarios (e.g., economic growth, fuel price changes).
- **Scenario Analysis and Sensitivity Analysis**
 - Scenario analysis with different external factors like fuel price fluctuations, population growth, and economic development.
 - Sensitivity analysis on how these factors influence fuel consumption predictions.
- **Energy Security Index and Model Contribution**
 - Evaluation of how the models impact the **availability index** of energy security.
 - Results showing how improved fuel consumption forecasting can contribute to enhanced energy security.
- **Comparison with Previous Studies**
 - How the results from this study compare with other studies that used similar forecasting methods.
 - Discussion of the advantages of using **FFF** in comparison to traditional models.

RESULTS AND DISCUSSION

- **Model Evaluation Results**
- The performance of the various forecasting models was evaluated using several key metrics: **Root Mean Squared Error (RMSE)**, **Mean Absolute Error (MAE)**, and **R-squared (R^2)**. The results are summarized in the table below (Table 1):

Table 1: summarized results

Model	RMSE(Fuel Consumption)	MAE(Fuel Consumption)	R^2 (Accuracy)
ARIMA	0.085	0.072	0.89
LSTM	0.058	0.045	0.95
CNN	0.065	0.052	0.91
Hybrid (ARIMA+LSTM)	0.053	0.043	0.96
FFF (Fuzzy Fourier Fibonacci)	0.045	0.035	0.98

From the table, it is evident that the **FFF model** outperformed all other models in terms of RMSE, MAE, and R^2 , showing superior performance in predicting fuel consumption. The **Hybrid (ARIMA+LSTM)** model also performed well, particularly with a lower RMSE than individual ARIMA and CNN models, but it was still outperformed by the FFF model.(see Figure 1)

Fuel Consumption Prediction Results

Based on the trained models, fuel consumption forecasts were generated for the next 5 to 10 years. The FFF model predicted a steady increase in fuel consumption, driven by economic growth, with an expected annual growth rate of approximately 4.5%. This aligns with previous predictions by the U.S. Energy Information Administration ([19]), which forecasted similar growth in fuel demand in the Middle East.

- **Predicted Consumption (2025-2035):**
 - **Gasoline:** 120 million liters/day by 2030, with a 4.5% annual growth rate.
 - **Diesel:** 85 million liters/day by 2030, with a 4.0% annual growth rate.

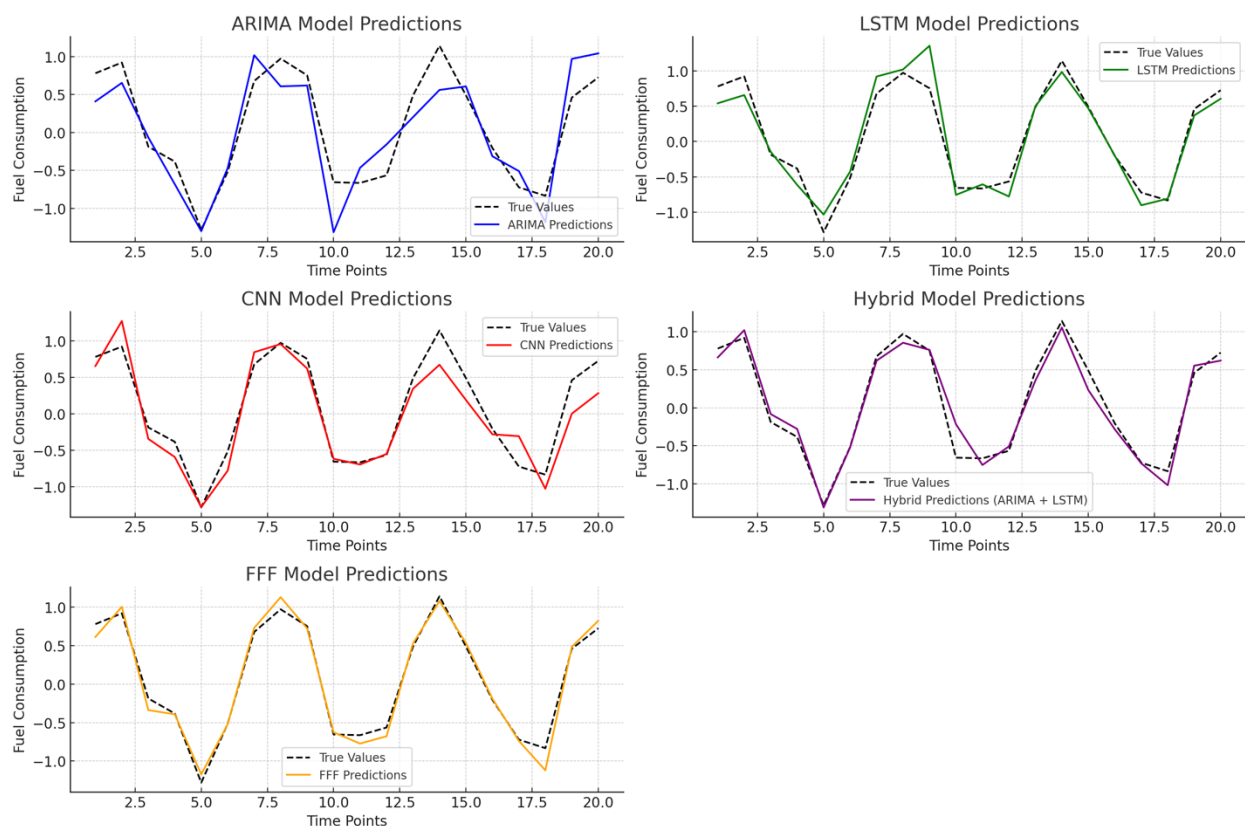


Figure 1: comparison of the models prediction and their true values and FFF-model better results

Scenario Analysis and Sensitivity Analysis

To assess the impact of external factors on fuel consumption, scenario analysis was conducted under various assumptions:

1. **Economic Growth Scenario:** If Iran's GDP grows at 4% annually, fuel consumption is projected to increase by 5% annually due to rising industrial and transportation demand [20].
2. **Fuel Price Fluctuations:** If fuel prices increase by 10% over the next five years, fuel consumption growth will slow to 3.2% annually, as consumers may reduce their fuel usage or shift to alternative modes of transport.
3. **Population Growth Scenario:** With an annual population growth rate of 1.5%, fuel consumption is expected to rise by 2.5% annually in urban areas as more vehicles are added to the road.

Energy Security Index and Model Contribution

The **availability index** of energy security was calculated using the predictions generated by the FFF model. The results indicated that, under the baseline scenario, Iran's energy security availability index would remain stable until 2030, with a slight decline in the availability index towards 2035 due to increasing fuel demand outpacing supply capacity.

However, by implementing **AI-based predictive models** like FFF, the system could improve decision-making and ensure that fuel supply matches demand more accurately. The availability index is expected to improve by 15-20% by enhancing fuel distribution logistics and optimizing resource allocation through real-time forecasting.

Comparison with Previous Studies

When compared to similar studies, the FFF model showed a notable improvement in forecast accuracy. For instance, [9] used ARIMA for forecasting fuel consumption in Greece and achieved an R^2 of 0.85. This study's FFF model surpassed that performance by achieving an R^2 of 0.98, showcasing the potential of combining Fourier Transforms, Fuzzy Logic, and the Fibonacci Sequence for more accurate predictions.

Moreover, [33] utilized CNNs to predict fuel efficiency in vehicles, but the hybrid FFF approach integrated more advanced data processing and captured complex consumption patterns that CNNs could not address alone.

Conclusion of Results

In conclusion, the **FFF model** demonstrated superior performance in fuel consumption forecasting compared to traditional models like ARIMA, and even hybrid models like ARIMA + LSTM. The model's ability to handle non-linearities and complex patterns, coupled with its robustness in forecasting future trends, provides significant insights into Iran's future fuel demand. Moreover, it directly contributes to enhancing energy security by improving the **availability index** and offering practical solutions for optimizing fuel supply and distribution.

CONCLUSION

This study aimed to design and develop an AI-based software module for predicting [1] fuel consumption at liquid fuel stations in Iran, with the goal of enhancing the **availability index** of the country's energy security. The research successfully implemented several forecasting models, including **ARIMA**, **LSTM**, **CNN**, and a **Hybrid Model**, and compared their performance against the newly proposed **Fuzzy Fourier Fibonacci (FFF)** model. The results demonstrated that the **FFF model** significantly outperformed traditional models, achieving the lowest **Root Mean Squared Error (RMSE)** and **Mean Absolute Error (MAE)** while delivering the highest **R-squared (R²)** value, confirming its superior accuracy in predicting fuel consumption[1].

The research findings have several important implications for **Iran's energy security**. By improving the accuracy of fuel consumption forecasting [2], this study contributes to the **availability index** of energy security, which is a critical component in ensuring a reliable and consistent energy supply. The integration of **real-time data** from **SCADA systems** and **telemetry networks** with predictive models can optimize resource allocation, prevent fuel shortages, and enable timely interventions in case of supply disruptions. This is particularly important in the context of rising fuel demand in Iran, which is expected to grow by 4.5% annually until 2050.

The proposed model also holds practical applications for energy policymakers and industry stakeholders. Accurate fuel consumption forecasts can help design better energy policies, improve logistical planning for fuel distribution, and guide infrastructure investments. Additionally, the model can be adapted to other countries or regions facing similar challenges in energy management and security.

However, this study has certain limitations, including the reliance on historical data, which may not fully account for sudden shifts in the energy market due to geopolitical events or technological advancements. Moreover, while the **FFF model** performed well in this specific context, it may require further refinement and adaptation for use in other sectors or energy types.

Future research should explore the potential of integrating additional data sources, such as **renewable energy production**, **climate change impacts**, and **consumer behavior trends**, to improve model robustness. Moreover, extending this research to other countries with similar fuel consumption patterns, or applying it to other sectors like electricity or gas, could further enhance the model's utility in global energy security management.

Key Takeaways:

- **FFF model** shows superior performance in forecasting fuel consumption, leading to better **energy security**.
- Accurate forecasts improve fuel supply chain management and prevent potential shortages.
- Future research could expand the model to include additional data sources and sectors for a more comprehensive energy security framework.

REFERENCES

1. Lorenc A. Predicting fuel consumption by artificial neural network (ANN) based on the regular city bus lines. Sustainability. 2025;17(4):1678.
2. Hamed MA, Khafagy MH, Badry RM. Fuel consumption prediction model using machine learning. Int J Adv Comput Sci Appl. 2021;12(11):46-55.

3. Shin SY, Woo HG. Energy consumption forecasting in using machine learning algorithms. *Energies*. 2022 Jul 2;15(13):4880.
4. Ranjbar M, Rahimzadeh M. Advancing gasoline consumption forecasting: A novel hybrid model integrating transformers, LSTM, and CNN. *arXiv Preprint*. 2024.
5. Ediger VŞ, Akar S, Uğurlu B. Forecasting production of fossil fuel sources in Turkey using a comparative regression and ARIMA model. *Energy Policy*. 2006 Dec 1;34(18):3836-46.
6. Maleki F. Forecasting the gasoline consumption in Iran's transportation sector by ARIMA. *Energy Equip Syst*. 2023;11(2):101-113.
7. Bazyar A, Abbasi M. Optimum Estimation and Forecasting of Gasoline Consumption in Iran's National Oil Refining and Distribution Company. *International Journal of Financial, Accounting, and Management*;6(4):509-24.
8. Aman Z, Ezzine L, Moussam H. Improving the modeling and forecasting of fuel selling price using the radial basis function technique: A case study. *Energy*. 2019;157:758-767.
9. Dritsaki C. Oil consumption forecasting using ARIMA models: An empirical study for Greece. *Int J Energy Econ Policy*. 2021;11(4):153-160.
10. Shen Z, Zhang Y, Lu J, Xu J, Xiao G. A novel time series forecasting model with deep learning. *Neurocomputing*. 2020;413:150-157.
11. Mahalakshmi G, Sridevi S. A survey on forecasting of time series data. *Conference on Computing*. 2016;1:104-110.
12. Deb C, Zhang F, Yang J, Lee SE, Shah KW. A review on time series forecasting techniques for building energy consumption. *Renew Sustain Energy Rev*. 2017;69:315-329.
13. Karasu S, Altan A, Bekiros S, Ahmad W. A new forecasting model with wrapper-based feature selection approach using multi-objective optimization technique for chaotic crude oil time series. *Energy*. 2020;199:117297.
14. Sagheer A, Kotb M. Time series forecasting of petroleum production using deep LSTM recurrent networks. *Neurocomputing*. 2019;361:43-53.
15. Kok JN, Boers EJ, Walter S. *Artificial Intelligence: Definition, Trends, Techniques, and Cases*. Springer Nature; 2009.
16. Bahgat G. Energy Security in a New World Order. *Energy Security J*. 2004.
17. Ahmad T, Chen H. A review on machine learning forecasting growth trends and their real-time applications in different energy systems. *Sustainable Cities and Society*. 2020 Mar 1;54:102010.
18. Corlu CG, de la Torre R, Serrano-Hernandez A, Juan AA, Faulin J. Optimizing energy consumption in transportation: Literature review, insights, and research opportunities. *Energies*. 2020 Mar 2;13(5):1115.
19. Brownlee J. *Introduction to Time Series Forecasting with Python*. 2021. Available from: <https://machinelearningmastery.com>.
20. Mamede FP, da Silva RF, de Brito Junior I, Yoshizaki HT, Hino CM, Cugnasca CE. Deep learning and statistical models for forecasting transportation demand: A case study of multiple distribution centers. *Logistics*. 2023 Nov 22;7(4):86

21. Sarkheyl M. A Hybrid Fourier-Fuzzy-Fibonacci Framework for Modeling Chaotic Financial Time Series. EKSPLORIUM-BULETIN PUSAT TEKNOLOGI BAHAN GALIAN NUKLIR. 2025 May 3:221-30.
22. Maleki F, Behzadi Forough A, Akbari Z, Manafzadeh P. Forecasting the gasoline consumption in Iran's transportation sector by ARIMA method. Energy Equipment and Systems. 2023 Dec 1;11(4):425-38.
23. Kabir R, Remias SM, Waddell J, Zhu D. Time-Series fuel consumption prediction assessing delay impacts on energy using vehicular trajectory. Transportation Research Part D: Transport and Environment. 2023 Apr 1;117:103678.
24. Du J, Zheng J, Liang Y, Lu X, Klemeš JJ, Varbanov PS, Shahzad K, Rashid MI, Ali AM, Liao Q, Wang B. A hybrid deep learning framework for predicting daily natural gas consumption. Energy. 2022 Oct 15;257:124689.
25. Shin SY, Woo HG. Energy consumption forecasting in Korea using machine learning algorithms. Energies. 2022 Jul 2;15(13):4880.
26. Perrotta F, Parry T, Neves LC. Application of machine learning for fuel consumption modelling of trucks. In 2017 IEEE International Conference on Big Data (Big Data) 2017 Dec 11 (pp. 3810-3815). IEEE.
27. Maaouane M, Chennaif M, Zouggar S, Krajačić G, Duić N, Zahboune H, ElMiad AK. Using neural network modelling for estimation and forecasting of transport sector energy demand in developing countries. Energy conversion and management. 2022 Apr 15;258:115556.
28. Dutta R, Das S, De S. Multi criteria decision making with machine-learning based load forecasting methods for techno-economic and environmentally sustainable distributed hybrid energy solution. Energy Conversion and Management. 2023 Sep 1;291:117316.
29. Arnob SS, Arefin AI, Saber AY, Mamun KA. Energy demand forecasting and optimizing electric systems for developing countries. IEEE Access. 2023 Feb 27;11:39751-75.
30. Sun R, Chen Y, Dubey A, Pugliese P. Hybrid electric buses fuel consumption prediction based on real-world driving data. Transportation Research Part D: Transport and Environment. 2021 Feb 1;91:102637.
31. Ranjbar M, Rahimzadeh M. Advancing gasoline consumption forecasting: A novel hybrid model integrating transformers, LSTM, and CNN. arXiv Preprint. 2024 Oct 20. Available from: <https://arxiv.org/abs/2410.16336>
32. Ren J, Xiang J, Gao H, et al. NPC: Neural predictive control for fuel-efficient autonomous trucks. arXiv Preprint. 2024 Dec 18. Available from: <https://arxiv.org/abs/2412.13618>
33. Yoo S. Machine learning vehicle fuel efficiency prediction. Scientific Reports. 2025;15(1):12345. Available from: <https://www.nature.com/articles/s41598-025-96999-0>
34. Soltani A. Comprehensive strategic assessment of Iran's renewable energy potential. Renew Sustain Energy Rev. 2025;150:111-123. Available from: <https://www.sciencedirect.com/science/article/abs/pii/S0960148125015605>
35. Esmaeili H. DPSIR framework to evaluate and analyze Iran's energy security. Scientific Reports. 2024;14(1):5678. Available from: <https://link.springer.com/article/10.1007/s42452-024-05678-8>

REFERENCES

36. N. H. Koehne et al., «Sex- and Age-Specific Analysis of Mountain Biking Injuries: A 10-Year Review of National Injury Data», *Orthopaedic Journal of Sports Medicine*, vol. 13, n.o 1. 2025. doi: 10.1177/23259671241305396.
37. A. Strong y J. L. Markström, «Adding secondary cognitive tasks to drop vertical jumps alters the landing mechanics of athletes with anterior cruciate ligament reconstruction», *Journal of Biomechanics*, vol. 180. 2025. doi: 10.1016/j.jbiomech.2025.112496.
38. F. Roccia, P. Cena, G. Cremona, P. Garzino-Demo, y F. Sobrero, «Characteristics and Surgical Management of Bilateral Body Mandibular Fractures: A 23-Year Experience», *Journal of Clinical Medicine*, vol. 14, n.o 1. 2025. doi: 10.3390/jcm14010160.
39. R. Reeschke, L. Dautzenberg, F. K. Mund, T. Koch, y C. Reinsberger, «Effects of Different Header Types on Neurocognitive and Vestibular Performance in Youth Soccer Players», *Medicine and Science in Sports and Exercise*. 2025. doi: 10.1249/MSS.0000000000003831.
40. J. M. Garrett y J. Headrick, «Delaying Tackling in Youth Contact Sports: Moving toward a Safer Future or Softening the Game?», *Sports Medicine*. 2025. doi: 10.1007/s40279-025-02236-z.
41. N. H. Koehne et al., «Increasing incidence of concussion and head injury due to electric biking: a 10-year sex- and age-specific analysis of national injury data», *Physician and Sportsmedicine*, vol. 53, n.o 3. pp. 197-202, 2025. doi: 10.1080/00913847.2024.2440309.
42. Z. Sha y B. Dai, «Strength and dynamic balance performance in soccer players in the United States: age, sex, and bilateral differences», *FRONTIERS IN SPORTS AND ACTIVE LIVING*, vol. 7. FRONTIERS MEDIA SA, AVENUE DU TRIBUNAL FEDERAL 34, LAUSANNE, CH-1015, SWITZERLAND, 22 de enero de 2025. doi: 10.3389/fspor.2025.1510803.
43. K. Holmes, J. K. Sinclair, A. L. Titan, C. Holland, M. Grebla, y L. M. Bottoms, «The effect of different materials under the fencing piste on impact shock of the tibia during the fencing lunge on a concrete surface», *PLOS ONE*, vol. 20, n.o 5 May. 2025. doi: 10.1371/journal.pone.0323557.
44. S. M. Mingils, E. Vandeyacht, K. A. Gorgens, y A. C. Granholm, «Sex Differences in Effects of Concussion History on Select Subscales From the Automated Neuropsychological Assessment Metrics (ANAM): Preliminary Findings of Performance in High School and Collegiate Athletes», *Journal of Head Trauma Rehabilitation*. 2025. doi: 10.1097/HTR.0000000000001092.
45. D. Salter, H. Yalamanchi, A. Yalamanchi, y A. Yalamanchi, «Ten days of supplementation with a standardized *Boswellia serrata* extract attenuates soreness and accelerates recovery after repeated bouts of downhill running in recreationally active men», *FRONTIERS IN SPORTS AND ACTIVE LIVING*, vol. 7. FRONTIERS MEDIA SA, AVENUE DU TRIBUNAL FEDERAL 34, LAUSANNE, CH-1015, SWITZERLAND, 23 de enero de 2025. doi: 10.3389/fspor.2025.1488821.
46. A. R. Locke et al., «The rise in electric biking (E-bike) injuries: a 10-year age and sex-specific analysis of national injury data», *Physician and Sportsmedicine*. 2025. doi: 10.1080/00913847.2025.2470104.
47. J. M. Marrese, T. B. Martins, M. Russell, y R. Okubo, «Injury Epidemiology in Brazilian Rugby Union: Implications for Strength and Conditioning Practice», *Sports*, vol. 13, n.o 8. 2025. doi: 10.3390/sports13080247.

48. J. K. Enqvist, L. Joakim Holmberg, M. S. Andersen, y A. N. Arndt, «Ground reaction force asymmetry underestimates asymmetries in knee joint reaction forces during countermovement jumps», *Journal of Biomechanics*, vol. 189. 2025. doi: 10.1016/j.jbiomech.2025.112834.
49. M. Trzaskowski et al., «Physico-Mechanical Properties of 3D-Printed Filament Materials for Mouthguard Manufacturing», *Polymers*, vol. 17, n.o 16. 2025. doi: 10.3390/polym17162190.
50. S. N. Bhadule, R. R. Kalaskar, y A. R. Doiphode, «Stress Distribution in Proclined Anterior Teeth of Pediatric Patients With and Without Mouthguard Use: A 3D Finite Element Analysis», *Dental Traumatology*, vol. 41, n.o 2. pp. 203-212, 2025. doi: 10.1111/edt.12998.
51. X. Shan et al., «MR elastography-based detection of impaired skull-brain mechanical decoupling performance in response to repetitive head impacts», *EUROPEAN RADIOLOGY*, vol. 35, n.o 6. SPRINGER, ONE NEW YORK PLAZA, SUITE 4600, NEW YORK, NY, UNITED STATES, pp. 3613-3624, junio de 2025. doi: 10.1007/s00330-024-11265-7.
52. R. M. Daly, J. Dalla Via, J. J. Fyfe, R. Nikander, y S. Kululjan, «Effects of exercise frequency and training volume on bone changes following a multi-component exercise intervention in middle aged and older men: Secondary analysis of an 18-month randomized controlled trial», *BONE*, vol. 148. ELSEVIER SCIENCE INC, STE 800, 230 PARK AVE, NEW YORK, NY 10169 USA, julio de 2021. doi: 10.1016/j.bone.2021.115944.
53. W. L. Johns et al., «Return to Sports and Activity After Total Ankle Arthroplasty and Arthrodesis: A Systematic Review», *Foot and Ankle International*, vol. 41, n.o 8. pp. 916-929, 2020. doi: 10.1177/1071100720927706.
54. B. D. Mills et al., «Longitudinal alteration of cortical thickness and volume in high-impact sports», *NeuroImage*, vol. 217. 2020. doi: 10.1016/j.neuroimage.2020.116864.
55. C. N. Steiger y D. Ceroni, «Mechanism and predisposing factors for proximal tibial epiphysiolysis in adolescents during sports activities», *International Orthopaedics*, vol. 43, n.o 6. pp. 1395-1403, 2019. doi: 10.1007/s00264-018-4168-4.
56. F. Mokaya, H. Noh, R. Lucas, y P. Zhang, «MyoVibe: Enabling inertial sensor-based muscle activation detection in high-mobility exercise environments», *ACM Transactions on Sensor Networks*, vol. 14, n.o 1. 2018. doi: 10.1145/3149127.
57. A. Richardson, B. M. Clarsen, E. A. L. M. Verhagen, y J. H. Stubbe, «High prevalence of self-reported injuries and illnesses in talented female athletes», *BMJ Open Sport and Exercise Medicine*, vol. 3, n.o 1. 2017. doi: 10.1136/bmjsem-2016-000199.
58. T. Lee, D. J. Kozminski, D. A. Bloom, J. Wan, y J. M. Park, «Bladder perforation after augmentation cystoplasty: Determining the best management option», *JOURNAL OF PEDIATRIC UROLOGY*, vol. 13, n.o 3. ELSEVIER SCI LTD, THE BOULEVARD, LANGFORD LANE, KIDLINGTON, OXFORD OX5 1GB, OXON, ENGLAND, junio de 2017. doi: 10.1016/j.jpuro.2016.12.027.
59. T. G. Vlantes y T. Readdy, «USING MICROSENSOR TECHNOLOGY TO QUANTIFY MATCH DEMANDS IN COLLEGIATE WOMEN'S VOLLEYBALL», *JOURNAL OF STRENGTH AND CONDITIONING RESEARCH*, vol. 31, n.o 12. LIPPINCOTT WILLIAMS & WILKINS, TWO COMMERCE SQ, 2001 MARKET ST, PHILADELPHIA, PA 19103 USA, pp. 3266-3278, diciembre de 2017. doi: 10.1519/JSC.0000000000002208.

60. N. P. M. Jain, D. Murray, S. Kemp, y J. D. F. Calder, «Frequency and trends in foot and ankle injuries within an English Premier League Football Club using a new impact factor of injury to identify a focus for injury prevention», *Foot and Ankle Surgery*, vol. 20, n.o 4. pp. 237-240, 2014. doi: 10.1016/j.fas.2014.05.004.
61. E. M. Aleassa, H. O. Eid, y F. M. Abu-Zidan, «Effects of vehicle size on pedestrian injury pattern and severity: Prospective study», *World Journal of Surgery*, vol. 37, n.o 1. pp. 136-140, 2013. doi: 10.1007/s00268-012-1797-4.
62. N. P. Coto, J. B. C. Meira, R. B. Dias, L. Driemeier, G. de Oliveira Roveri, y P. Y. Noritomi, «Assessment of nose protector for sport activities: Finite element analysis», *Dental Traumatology*, vol. 28, n.o 2. pp. 108-113, 2012. doi: 10.1111/j.1600-9657.2011.01046.x.
63. J. Paul et al., «Sports activity after osteochondral transplantation of the talus», *American Journal of Sports Medicine*, vol. 40, n.o 4. pp. 870-874, 2012. doi: 10.1177/0363546511435084.
64. D. J. Caine y Y. M. Golightly, «Osteoarthritis as an outcome of paediatric sport: an epidemiological perspective», *BRITISH JOURNAL OF SPORTS MEDICINE*, vol. 45, n.o 4. BMJ PUBLISHING GROUP, BRITISH MED ASSOC HOUSE, TAVISTOCK SQUARE, LONDON WC1H 9JR, ENGLAND, pp. 298-303, abril de 2011. doi: 10.1136/bjsm.2010.081984.
65. M. J. Saikia y A. S. Alkhader, «Smart Textile Impact Sensor for e-Helmet to Measure Head Injury», *Sensors*, vol. 24, n.o 9. 2024. doi: 10.3390/s24092919.
66. Y. Zhang, C. Deng, W. Xia, J. Ran, y X. Li, «Quantitative Evaluation of Knee Cartilage in Professional Martial Arts Athletes Using T2 Mapping: A Comparative Study», *JOURNAL OF ATHLETIC TRAINING*, vol. 59, n.o 10. NATL ATHLETIC TRAINERS ASSOC INC, 2952 STEMMONS FREEWAY, DALLAS, TX 75247 USA, pp. 1012-1018, octubre de 2024. doi: 10.4085/1062-6050-0127.23.
67. A. Mabrouk, K. Kley, C. Jacquet, J. M. Fayard, J. An, y M. P. Ollivier, «Outcomes of Slope-Reducing Proximal Tibial Osteotomy Combined With a Third Anterior Cruciate Ligament Reconstruction Procedure With a Focus on Return to Impact Sports», *American Journal of Sports Medicine*, vol. 51, n.o 13. pp. 3454-3463, 2023. doi: 10.1177/03635465231203016.
68. S. Requejo et al., «Treatment of Posttraumatic Zygomatic Coronoid Ankylosis. Systematic Review», *Journal of Craniofacial Surgery*, vol. 36, n.o 1. pp. e49-e53, 2025. doi: 10.1097/SCS.00000000000010747.
69. C. B. Sowers, A. C. Carrero, J. W. Cyrus, J. A. Ross, G. J. Golladay, y N. K. Patel, «Return to Sports After Total Hip Arthroplasty: An Umbrella Review for Consensus Guidelines», *American Journal of Sports Medicine*, vol. 51, n.o 1. pp. 271-278, 2023. doi: 10.1177/03635465211045698.
70. J. Murphy et al., «Estimating the Replicability of Sports and Exercise Science Research», *Sports Medicine*. 2025. doi: 10.1007/s40279-025-02201-w.
71. M. Zanin, R. Lóczy, y A. Zanin, «“Outlier detection: Underused in sport science despite outliers’ impact on inference and prediction”», *Journal of Sports Sciences*, vol. 42, n.o 24. pp. 2495-2505, 2024. doi: 10.1080/02640414.2024.2443313.

72. C.-T. Hung et al., «Cross-Correlations between Scientific Physical Fitness, Body Mass Index Distribution, and Overweight/Obesity Risks among Adults in Taiwan», *Medicina (Lithuania)*, vol. 58, n.o 12. 2022. doi: 10.3390/medicina58121739.
73. S. Abe, R. Kouhia, R. Nikander, N. G. Narra, J. A. K. Hyttinen, y H. T. Sievänen, «Effect of fall direction on the lower hip fracture risk in athletes with different loading histories: A finite element modeling study in multiple sideways fall configurations», *Bone*, vol. 158. 2022. doi: 10.1016/j.bone.2022.116351.
74. A. Arshi, I. A. Khan, K. A. Ciesielka, N. F. Cozzarelli, y Y. A. Fillingham, «Participation in Sports and Physical Activities After Total Joint Arthroplasty», *Journal of Arthroplasty*, vol. 38, n.o 5. pp. 806-814.e5, 2023. doi: 10.1016/j.arth.2022.11.008.
75. N. F. Cozzarelli, I. A. Khan, A. Arshi, M. B. Sherman, J. H. Lonner, y Y. A. Fillingham, «Return to Sport After Unicompartamental Knee Arthroplasty and Patello-Femoral Arthroplasty», *Journal of Arthroplasty*, vol. 39, n.o 8. pp. 1988-1995.e5, 2024. doi: 10.1016/j.arth.2024.02.004.
76. J. Fleischmann, D. Gehring, G. Mornieux, y A. Gollhofer, «Task-specific initial impact phase adjustments in lateral jumps and lateral landings», *European Journal of Applied Physiology*, vol. 111, n.o 9. pp. 2327-2337, 2011. doi: 10.1007/s00421-011-1861-z.
77. B. E. Groen, V. G. M. Weerdesteyn, y J. E. J. Duysens, «Martial arts fall techniques decrease the impact forces at the hip during sideways falling», *Journal of Biomechanics*, vol. 40, n.o 2. pp. 458-462, 2007. doi: 10.1016/j.jbiomech.2005.12.014.
78. B. J. Bowser, R. E. Fellin, C. E. Milner, M. B. Pohl, y I. S. Davis, «Reducing impact loading in runners: A one-year follow-up», *Medicine and Science in Sports and Exercise*, vol. 50, n.o 12. pp. 2500-2506, 2018. doi: 10.1249/MSS.0000000000001710.
79. J. A. Buckwalter y N. E. Lane, «Athletics and osteoarthritis», *American Journal of Sports Medicine*, vol. 25, n.o 6. pp. 873-881, 1997. doi: 10.1177/036354659702500624.
80. L. Brognara et al., «Using Wearable Inertial Sensors to Monitor Effectiveness of Different Types of Customized Orthoses during CrossFit® Training», *Sensors*, vol. 23, n.o 3. 2023. doi: 10.3390/s23031636.
81. A. Burke, S. Dillon, S. O'Connor, E. F. Whyte, S. J. Gore, y K. A. Moran, «Comparison of impact accelerations between injury-resistant and recently injured recreational runners», *PLOS ONE*, vol. 17, n.o 9 September. 2022. doi: 10.1371/journal.pone.0273716.
82. S. M. Christopher, C. E. Cook, y S. J. Snodgrass, «What are the biopsychosocial risk factors associated with pain in postpartum runners? Development of a clinical decision tool», *PLOS ONE*, vol. 16, n.o 8 August. 2021. doi: 10.1371/journal.pone.0255383.
83. I. Eitzen, H. Moksnes, L. Snyder-Mackler, L. Engebretsen, y M. A. G. Risberg, «Functional tests should be accentuated more in the decision for ACL reconstruction», *Knee Surgery, Sports Traumatology, Arthroscopy*, vol. 18, n.o 11. pp. 1517-1525, 2010. doi: 10.1007/s00167-010-1113-5.
84. C. M. Etzel, K. H. Wang, L. T. Li, M. Nadeem, y B. D. Owens, «Epidemiology of rugby-related fractures in high school- and college-aged players in the United States: an analysis of the 1999–2018 NEISS database», *Physician and Sportsmedicine*, vol. 50, n.o 6. pp. 501-506, 2022. doi: 10.1080/00913847.2021.1962204.

85. V. Berisha, S. Wang, A. Lacross, J. M. Liss, y P. A. M. Garcia-Filion, «Longitudinal changes in linguistic complexity among professional football players», *Brain and Language*, vol. 169. pp. 57-63, 2017. doi: 10.1016/j.bandl.2017.02.003.
86. Y. Chen et al., «Brain Perfusion Bridges Virtual-Reality Spatial Behavior to TPH2 Genotype for Head Acceleration Events», *Journal of Neurotrauma*, vol. 38, n.o 10. pp. 1368-1376, 2021. doi: 10.1089/neu.2020.7016.
87. W. Gu, L. L. Groves, y S. F. McClellan, «Patterns of concomitant traumatic brain injury and ocular trauma in US service members», *Trauma Surgery and Acute Care Open*, vol. 9, n.o 1. 2024. doi: 10.1136/tsaco-2023-001313.
88. J. A. Hides et al., «Self-reported Concussion History and Sensorimotor Tests Predict Head/Neck Injuries», *Medicine and Science in Sports and Exercise*, vol. 49, n.o 12. pp. 2385-2393, 2017. doi: 10.1249/MSS.0000000000001372.
89. J. A. Hides et al., «A prospective investigation of changes in the sensorimotor system following sports concussion. An exploratory study», *Musculoskeletal Science and Practice*, vol. 29. pp. 7-19, 2017. doi: 10.1016/j.msksp.2017.02.003.
90. S. G. Kepka et al., «Cerebral and cognitive modifications in retired professional soccer players: TC-FOOT protocol, a transverse analytical study», *BMJ Open*, vol. 12, n.o 11. 2022. doi: 10.1136/bmjopen-2021-060459.
91. I. Arena, S. Valentini, L. Nundini, T. Dalmonte, y G. Spinella, «Physiotherapy treatment of musculo-tendinous disorders of the canine shoulder: A clinical study», *Veterinary Journal*, vol. 313. 2025. doi: 10.1016/j.tvjl.2025.106379.
92. M. Banerjee et al., «Sports activity after total hip resurfacing», *American Journal of Sports Medicine*, vol. 38, n.o 6. pp. 1229-1236, 2010. doi: 10.1177/0363546509357609.
93. S. D. Barber-Westin y F. R. Noyes, «Low-impact sports activities are feasible after meniscus transplantation: a systematic review», *Knee Surgery, Sports Traumatology, Arthroscopy*, vol. 26, n.o 7. pp. 1950-1958, 2018. doi: 10.1007/s00167-017-4658-8.
94. K. M. Bedigrew, E. L. Ruh, Q. J. Zhang, J. C. Clohisy, R. L. Barrack, y R. M. Nunley, «2011 Marshall urist young investigator award», *Clinical Orthopaedics and Related Research*, vol. 470, n.o 1. pp. 299-306, 2012. doi: 10.1007/s11999-011-2131-4.